

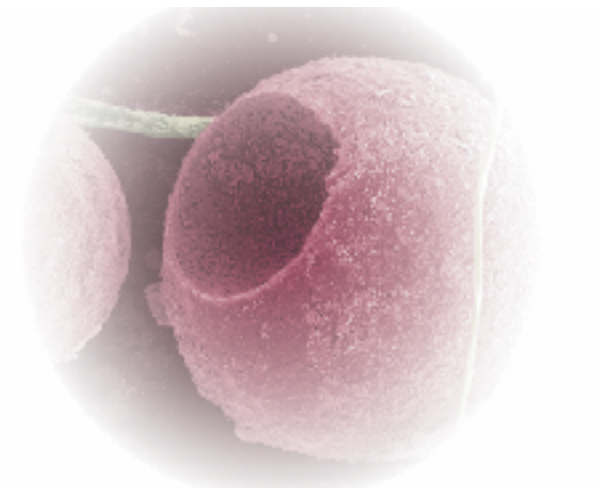
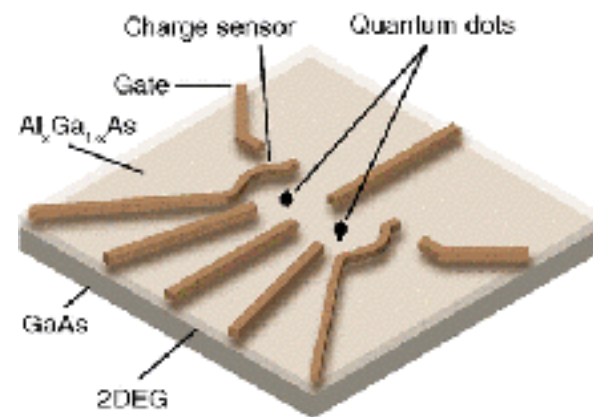
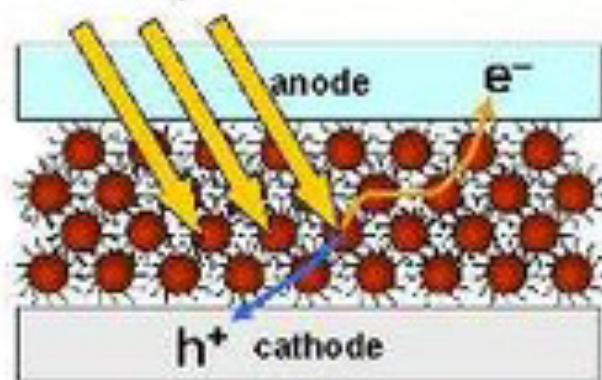
Speeding up computational geometry optimization using statistical methods and neural networks

GM20171219 Presentation - Xiang Zhang

Motivation: Quantum Dots and Nanostructures

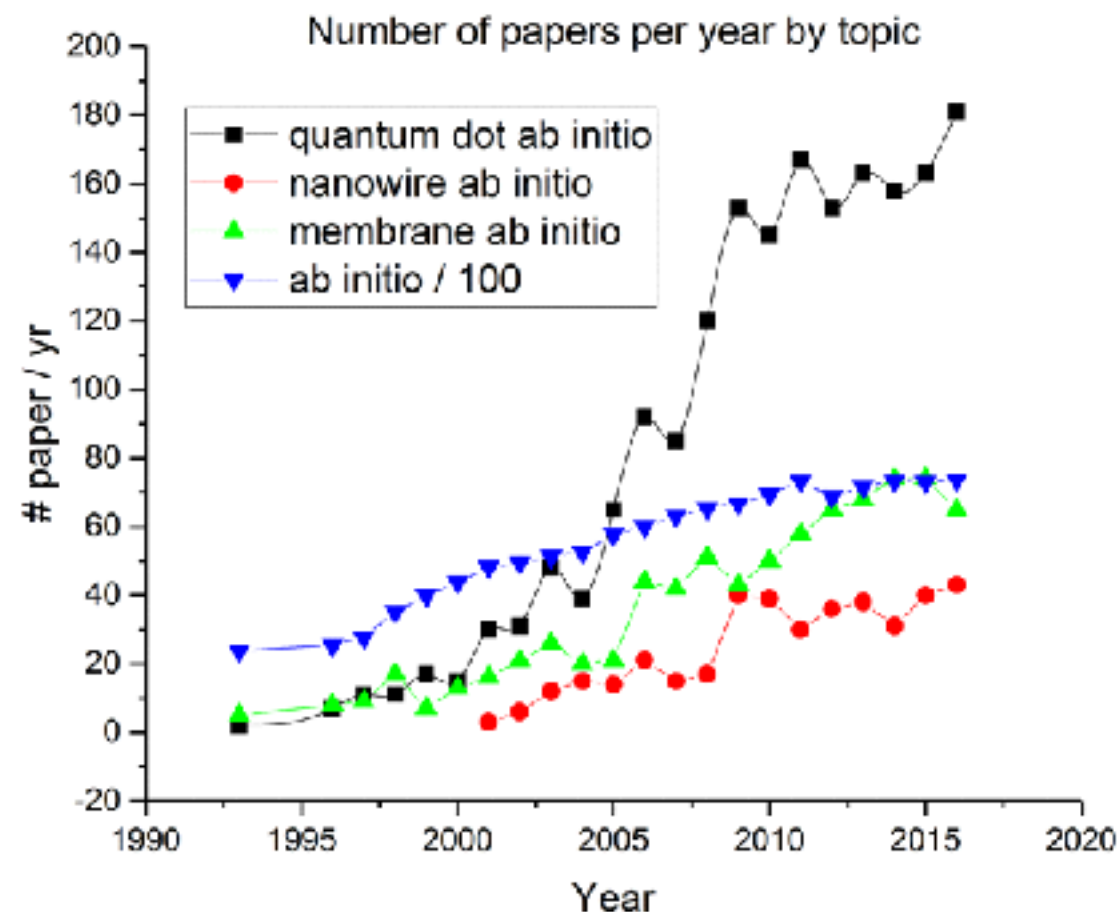
- Quantum dots have optoelectronic and biological applications, and are fundamentally interesting.

colloidal quantum dot solar cell



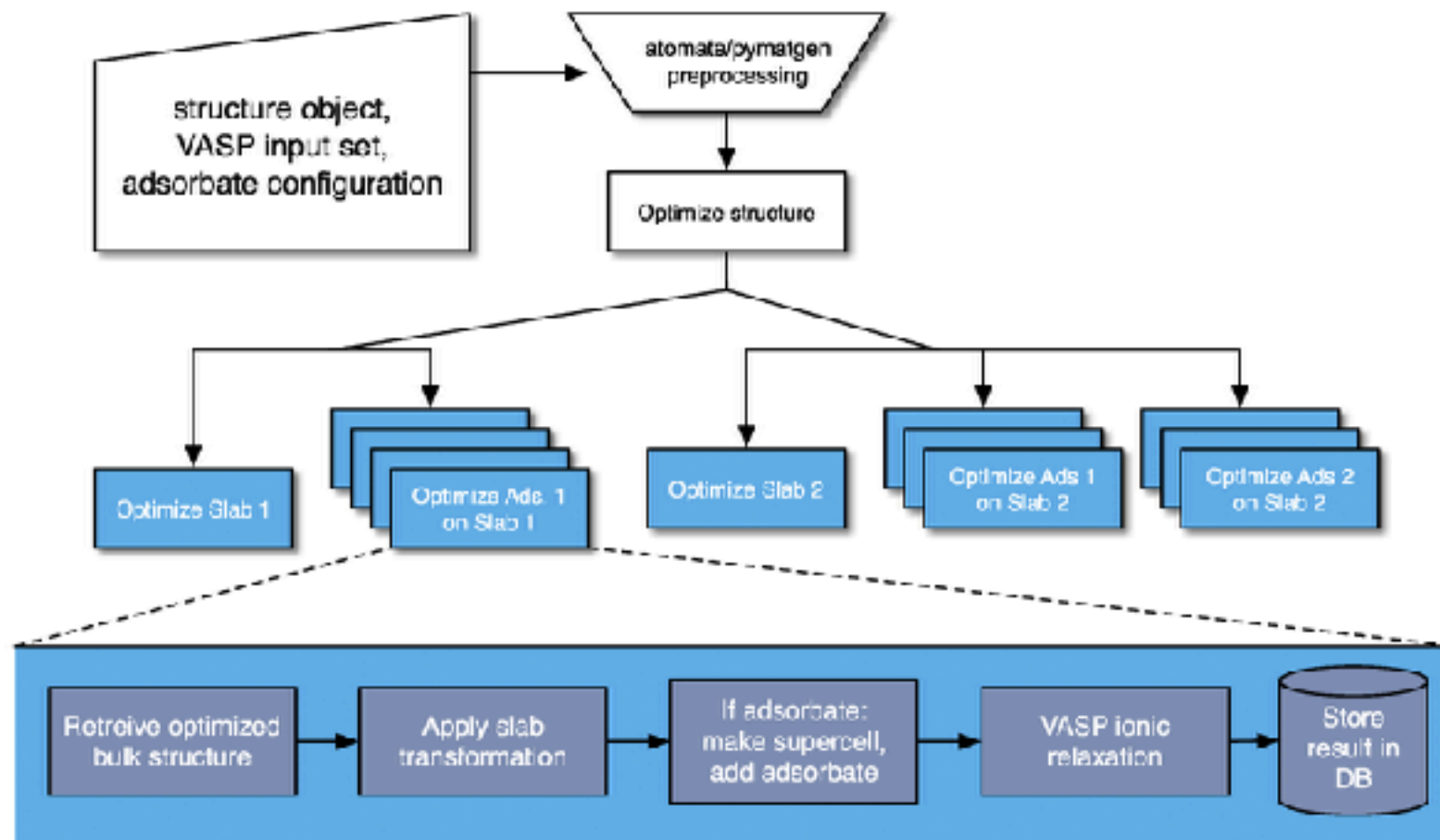
Motivation: Quantum Dots and Nanostructures

- Quantum dots have optoelectronic and biological applications, and are fundamentally interesting.
- Computational research on non-crystalline structures are on the rise.



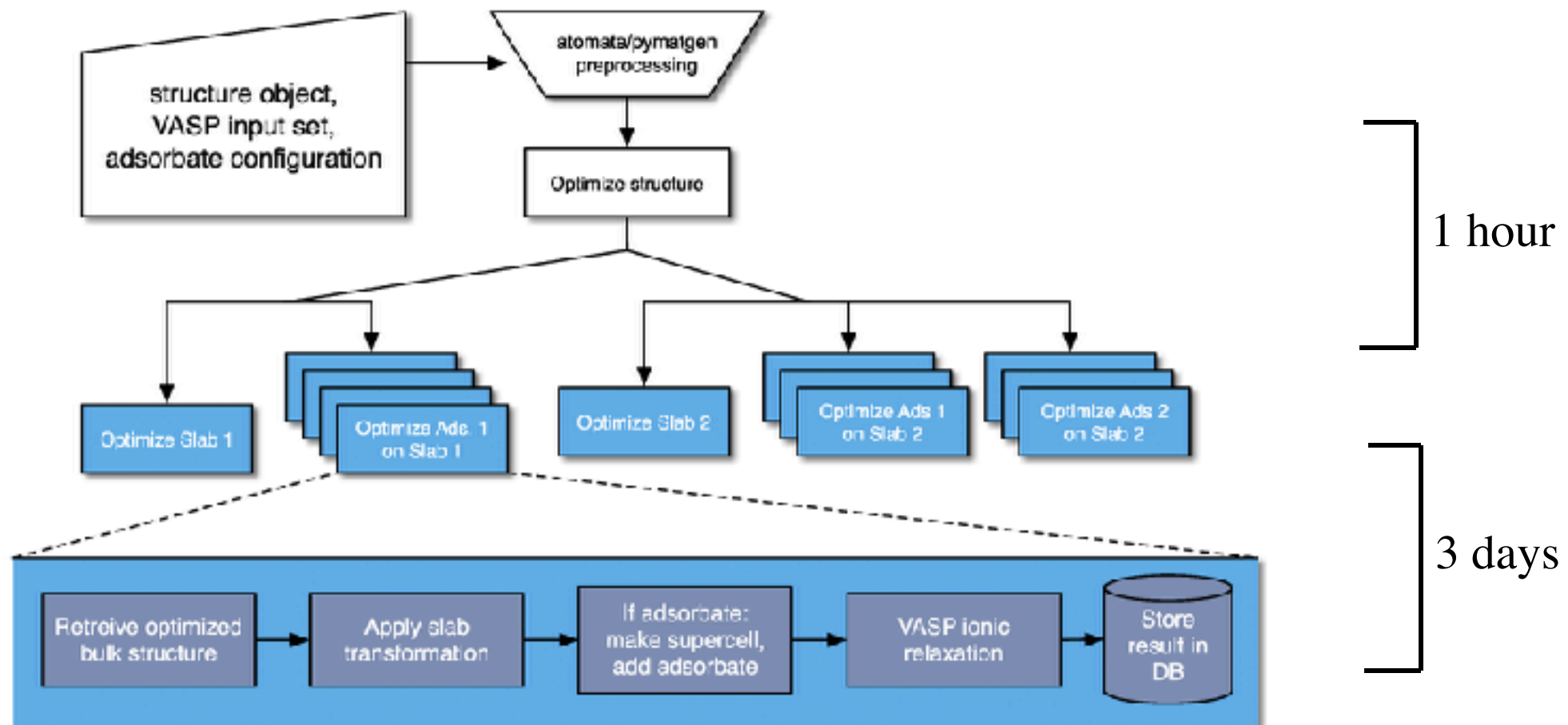
Motivation: Geometry Optimization is Slow

- Computational workflow: optimize \rightarrow electronic structure



Motivation: Geometry Optimization is Slow

- Computational workflow: optimize → electronic structure
- Computing band structure takes 1 self-consistent step. Geometry optimization can take 200.

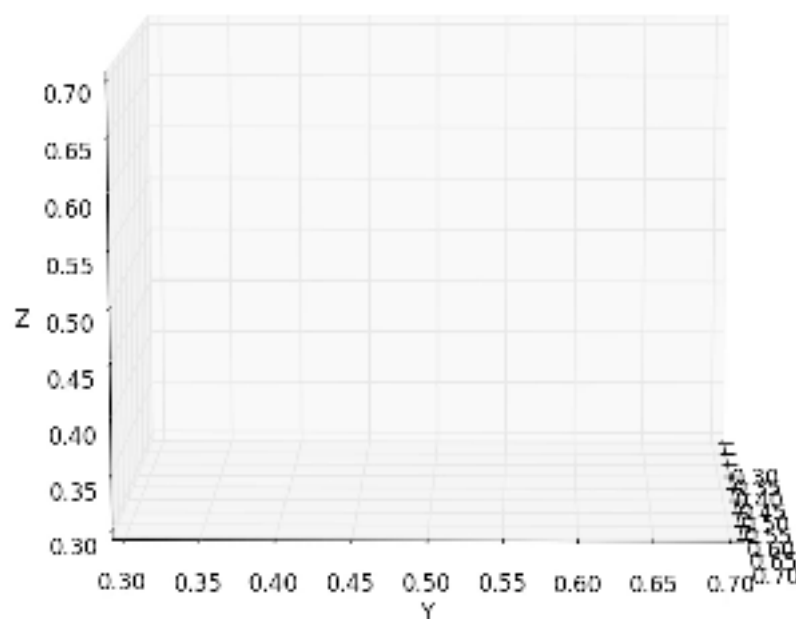


Motivation: Geometry Optimization is Learnable

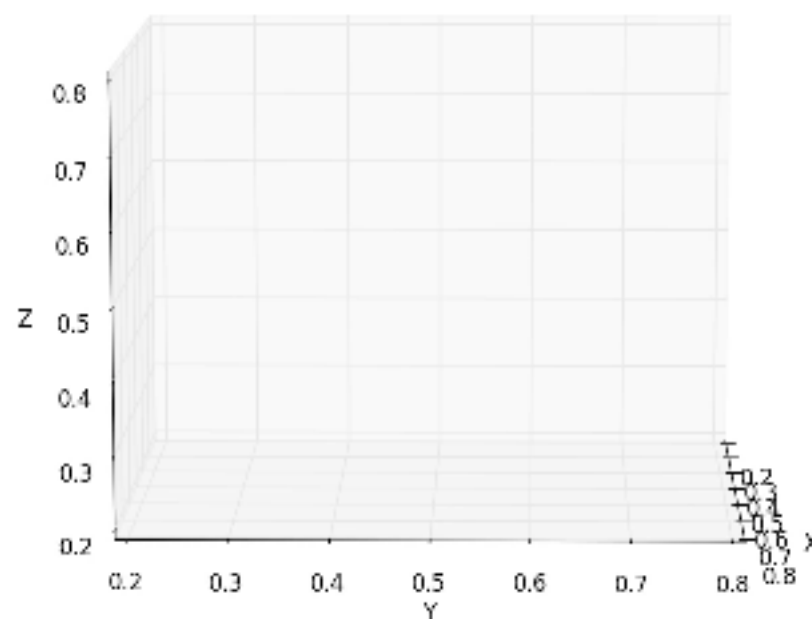
In geometry optimization, atoms are incrementally moved towards the lowest energy configuration.

Here are some trajectories.

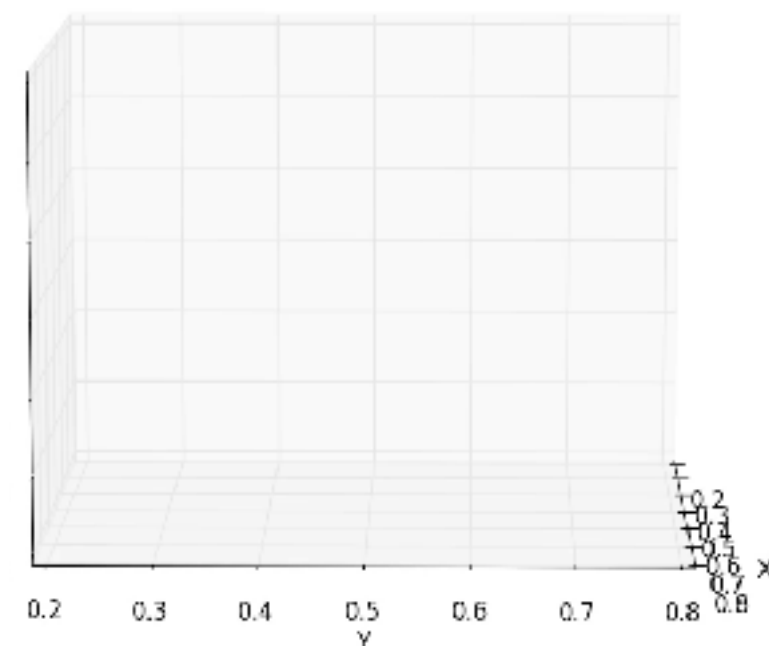
Pb62S63



Pb108S108

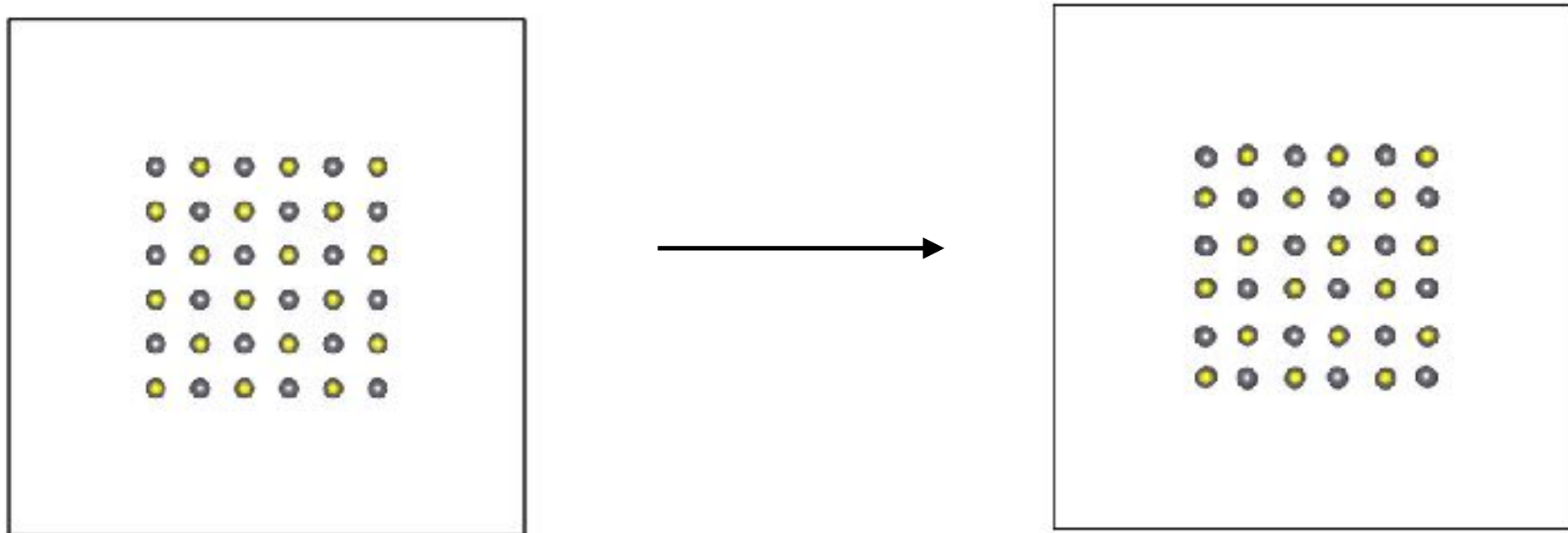


Pb172S171



Problem Statement

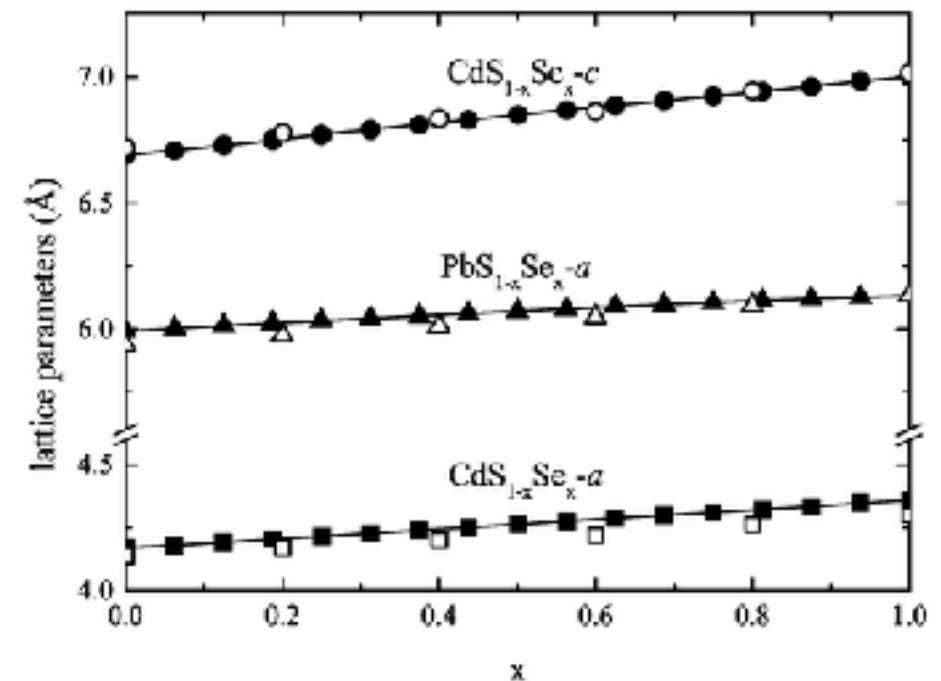
- Predict optimized coordinates from starting coordinates.
- Capture physically insignificant, small optimizations ($<0.3 \text{ \AA}$).
- Work with relatively few data ($\sim 10^1$ runs).



Background: Available Force Fields

- Conventional molecular mechanics force fields
 - No commercially available ones for Pb and S
 - Not fitted to nanostructures & not accurate enough

force on one complex	RMS error (kcal/mol/Å)
composite	19.6
dot size 1	21.4
dot size 2	23.0
dot size 3	16.8
dot size 4	20.9
dot size 5	18.6



Background: Available Force Fields

- Conventional force fields
 - No commercially available ones for PbS
 - Some active research going on
- Neural network potentials
 - Recipes exist, but no ready-made ones for PbS
 - $0.1\text{eV} / \text{\AA}$ force accuracy at 10^4 data points

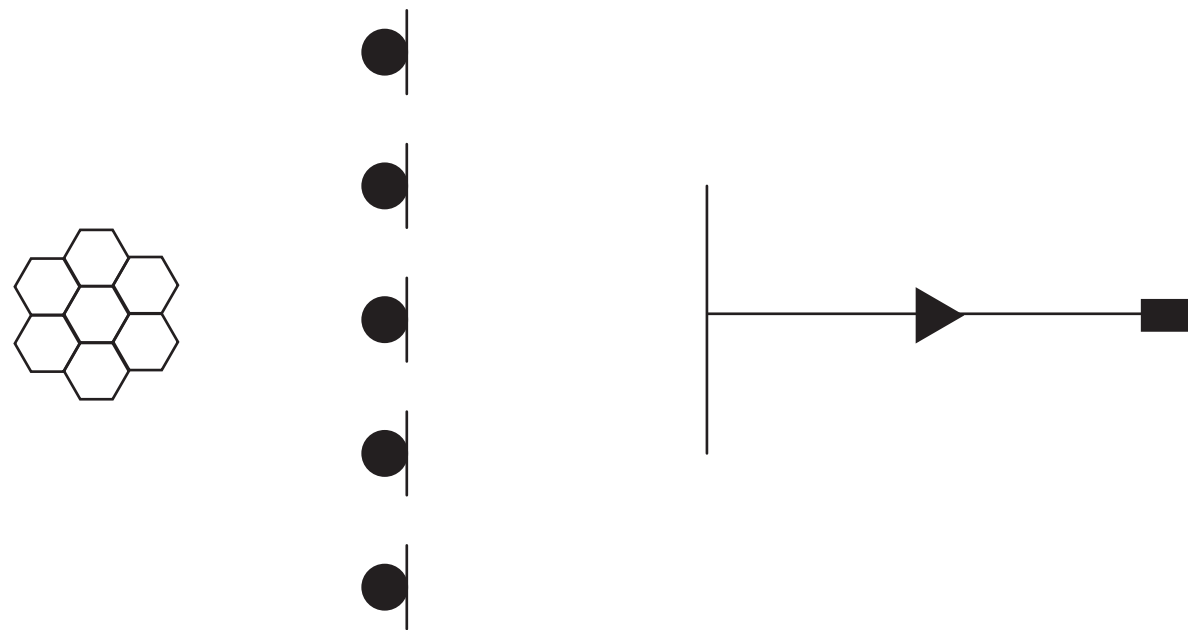
Background: the Canonical NN potential

$$\overrightarrow{X_1}, \overrightarrow{X_2}, \dots, \overrightarrow{X_n} \rightarrow f_1, f_2, \dots, f_m \rightarrow E \mid \vec{F} \rightarrow \overrightarrow{dX}$$

Symmetry function features:

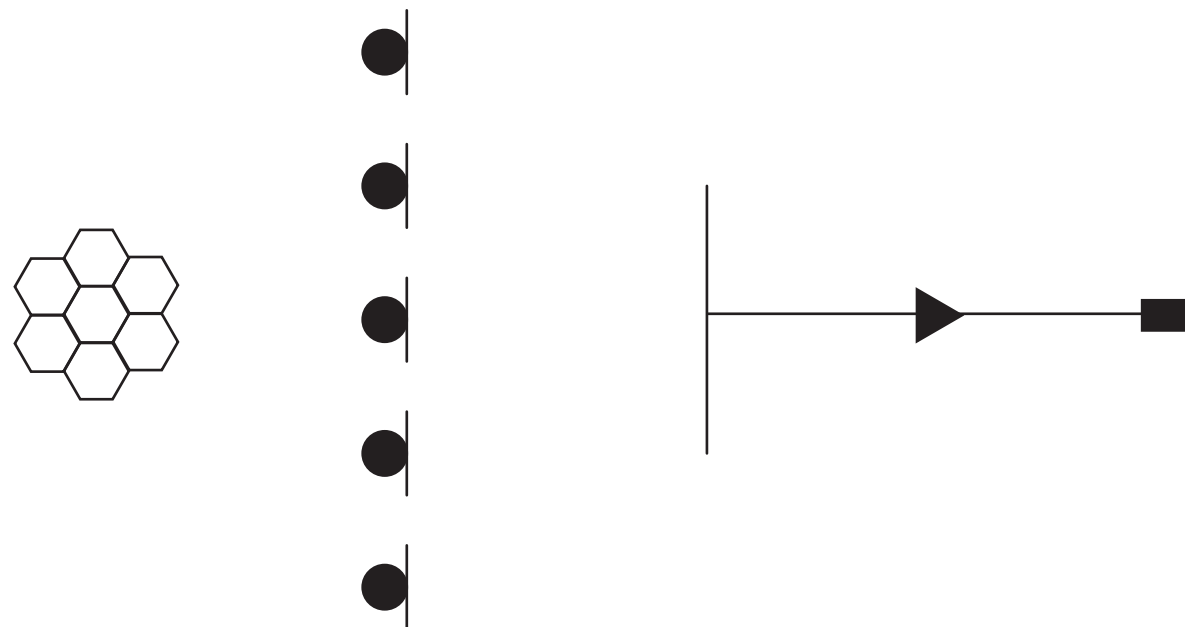
$$f_2 = \sum_{i,j} (1 + \lambda \cos \theta_{ij})^\zeta e^{-\eta(r_i^2 + r_j^2)} \cos \pi \left(\frac{r_i}{R_C} + 1 \right) \cos \pi \left(\frac{r_j}{R_C} + 1 \right)$$

$$E = ANN(f_2), \vec{F} = -\frac{\partial E}{\partial \vec{x}}$$



Model

$$\overrightarrow{X_1}, \overrightarrow{X_2}, \dots, \overrightarrow{X_n} \rightarrow f_1, f_2, \dots, f_m \rightarrow E \mid \vec{F} \rightarrow \overrightarrow{dX}$$



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$$E = ANN(f_2), \vec{F} = -\frac{\partial E}{\partial \vec{x}}$$

Every permutationally invariant function can be expressed as a cluster expansion of functions representable by neural nets:

$$E = \sum_i h_1(x_i) + \sum_{ij} h_2(x_i, x_j) + \dots$$

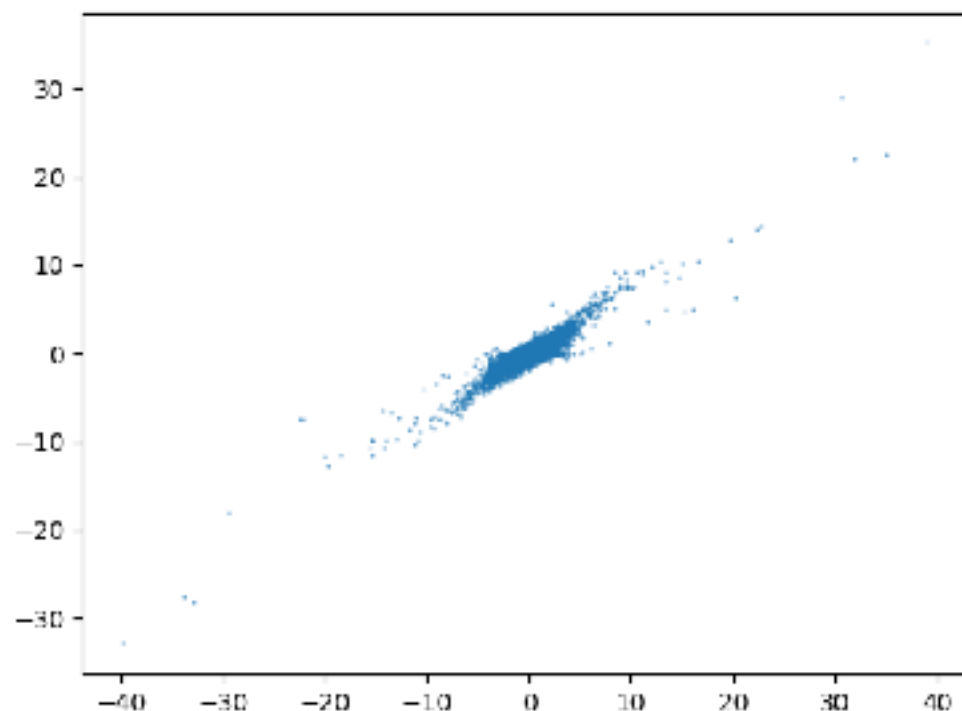
Components of a normal sum does not 'interact' with each other. Thus 1-order cluster expansion accounts for 1-body interaction.

LSTM neural networks can add long-range correlation as well as alleviate exploding gradients in long sums.

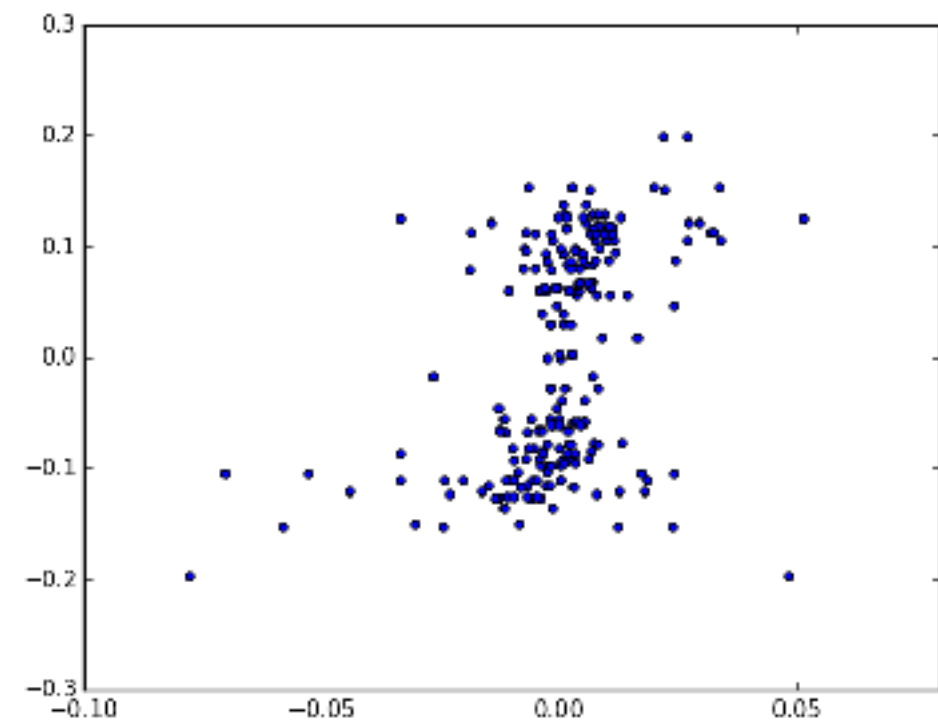
$$E_{LSTM} = \sum_i^{LSTM} h(x_i)$$

Result: $F(\{\mathbf{x}_i\})$ and $\mathbf{dx}(\{\mathbf{x}_i\})$

Predicted vs. actual forces



Predicted vs. actual optimized coordinates
(time per run $\sim 4\text{h}$)

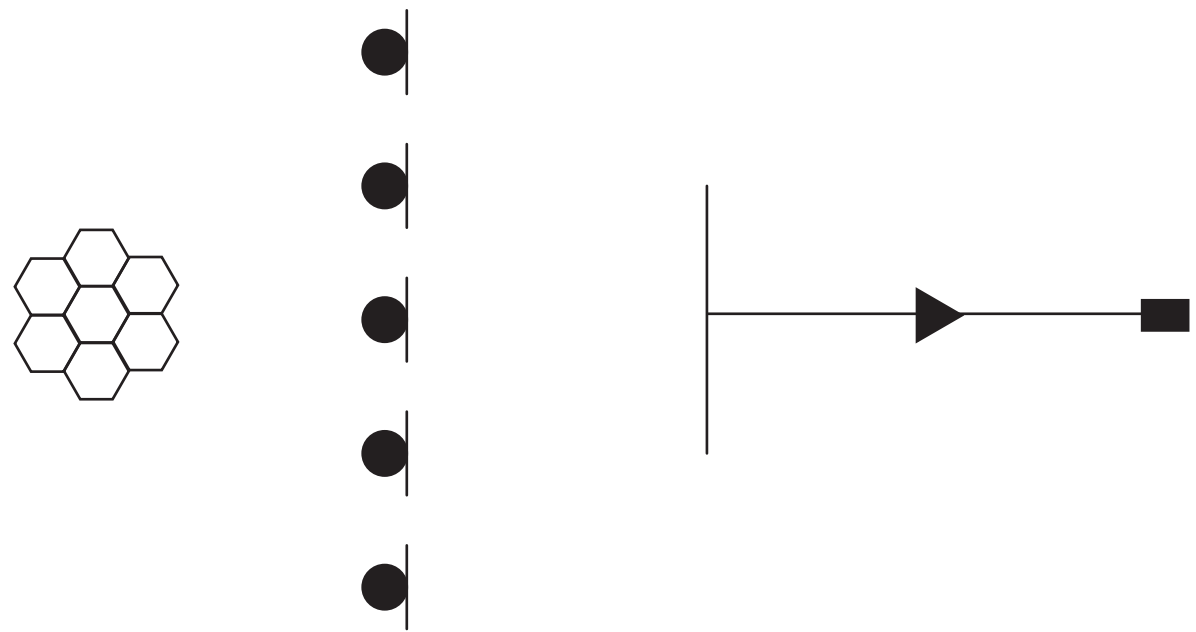


Training set: 91 quantum dots (single-point force calculation).

Test set: 1 quantum dot (geometry optimization).

Model

$$\overrightarrow{X_1}, \overrightarrow{X_2}, \dots, \overrightarrow{X_n} \rightarrow \overrightarrow{dx}$$



For $dx(\{x_i\})$, coordinates are discrete. Instead of learning a infinite-degree-of-freedom function, we now only have to learn a finite set of values.

$$\overrightarrow{dx} = \sum_i \overrightarrow{h_1}(x_i) = \sum_i \overrightarrow{h_i}$$

Symmetries can be included:

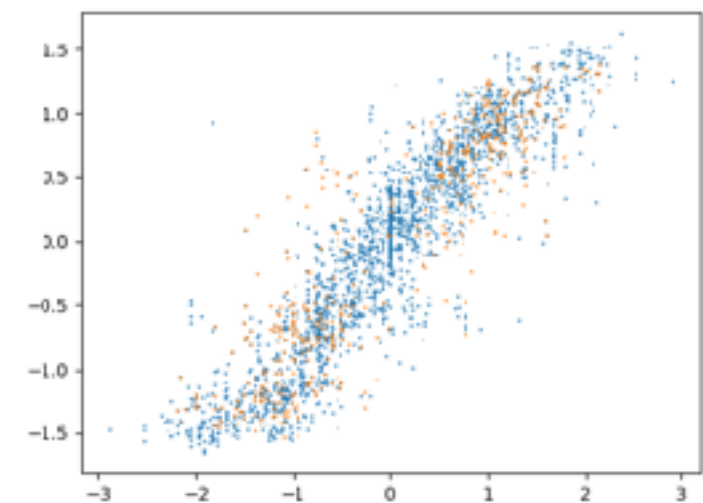
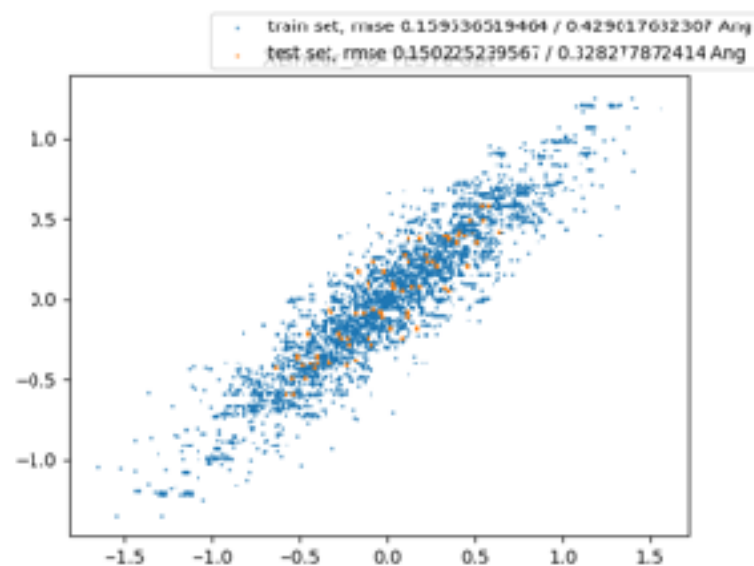
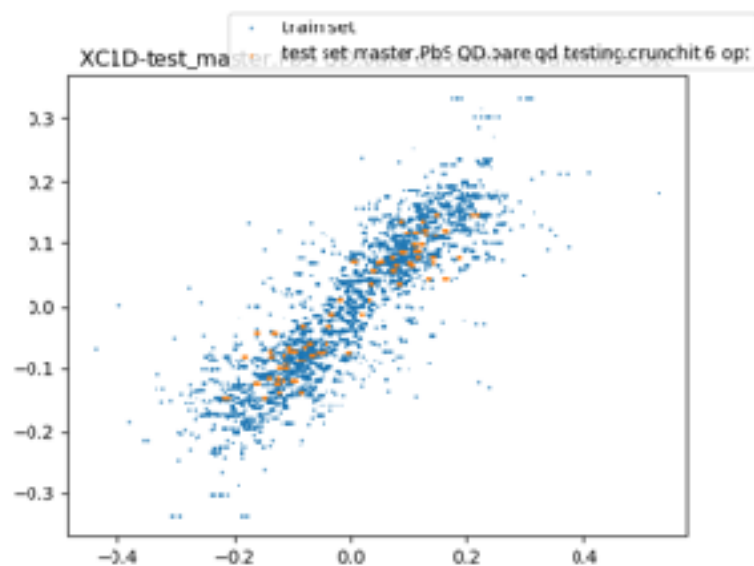
$$\overrightarrow{dx}(\overrightarrow{x_i}) = dx(|x_i|) \cdot \widehat{x_i}$$

which is extendable to higher dimensions:

$$h_{x_i, x_j} = h_{ij1} \widehat{x_i} + h_{ij2} \widehat{x_j} + h_{ij3} (\widehat{x_i} \times \widehat{x_j})$$

Result: $dx(\{x_i\})$

Predicted vs. actual $(x_i - x_i^0) / \text{\AA}$, training and test set



Training set: 13 quantum dots (geometry optimization).

Test set: 1 quantum dot (geometry optimization).

Time per run: $\sim 20s$

Summary

- Machine learning models (MLP, LSTM, Lasso) for pre-optimizing quantum dot structures
- Small range, high accuracy, low data requirement, at the cost of generality

Thank you